For a sphere with radius $r$, the volume is found using $V=\frac{4}{3} \pi r^{3}$.
For more information, see the Math Notes box in Lesson 10.1.5
of the Core Connections, Course 3 text.

## Example 1

Find the volume of the sphere at right.

$$
\begin{gathered}
V=\frac{4}{3} \pi r^{3}=\frac{4}{3} \pi \cdot 2^{3}=\frac{32 \pi}{3} \mathrm{ft}^{3} \text { (exact answer) } \\
\quad \text { or using } \pi \approx 3.14, \\
\frac{32(3.14)}{3} \approx 33.49 \mathrm{ft}^{3}(\text { approximate answer })
\end{gathered}
$$



## Example 2

A sphere has a volume of $972 \pi$ un. $^{3}$. Find the radius.
Use the formula for volume and solve the equation for the radius.

$$
\begin{array}{ll}
V=\frac{4}{3} \pi r^{3}=972 \pi & \text { Substitution. } \\
4 \pi r^{3}=2916 \pi & \text { Multiply by } 3 \text { to remove the fraction } . \\
r^{3}=\frac{2916 \pi}{4 \pi}=729 & \text { Divide by } 4 \pi \text { to isolate } r . \\
r=\sqrt[3]{729}=9 & \text { To undo cubing, take the cube root. }
\end{array}
$$

## Problems

Use the given information to find the exact and approximate volume of the sphere.

1. radius $=10 \mathrm{~cm}$
2. radius $=4 \mathrm{ft}$
3. diameter $=10 \mathrm{~cm}$
4. $\quad$ diameter $=3$ miles
5. circumference of great circle $=12 \pi$ un.
6. circumference of great circle $=3 \pi$ un.

Use the given information to answer each question related to spheres.
7. If the radius is 7 cm , find the volume.
8. If the diameter is 10 inches, find the volume.
9. If the volume of the sphere is $36 \pi$ un. ${ }^{3}$, find the radius.
10. If the volume of the sphere is $\frac{256 \pi}{3}$ un. $^{3}$, find the radius.

## Answers

1. $\frac{4000 \pi}{3} \approx 4186.67 \mathrm{~cm}^{3}$
2. $\frac{500 \pi}{3} \approx 523.33 \mathrm{~cm}^{3}$
3. $288 \pi \approx 904.32$ un. $^{3}$
4. $\frac{1372 \pi}{3} \approx 1436.75 \mathrm{~cm}^{3}$
5. $r=3$ units
6. $\frac{256 \pi}{3} \approx 267.94 \mathrm{ft}^{3}$
7. $\frac{9 \pi}{2} \approx 14.13 \mathrm{mi}^{3}$
8. $\frac{9 \pi}{2} \approx 14.13 \mathrm{mi}^{3}$
9. $\frac{500 \pi}{3} \approx 523.60 \mathrm{in}^{3}$
10. $r=4$ units
