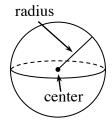
For a sphere with radius r, the volume is found using $V = \frac{4}{3} \pi r^3$.

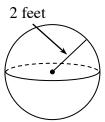
For more information, see the Math Notes box in Lesson 10.1.5 of the *Core Connections*, *Course 3* text.



Example 1

Find the volume of the sphere at right.

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \cdot 2^3 = \frac{32\pi}{3} \text{ ft}^3 \text{ (exact answer)}$$
or using $\pi \approx 3.14$,
$$\frac{32(3.14)}{3} \approx 33.49 \text{ ft}^3 \text{ (approximate answer)}$$



Example 2

A sphere has a volume of 972π un.³. Find the radius.

Use the formula for volume and solve the equation for the radius.

$$V = \frac{4}{3}\pi r^3 = 972\pi$$

Substitution.

$$4\pi r^3 = 2916\pi$$

Multiply by 3 to remove the fraction.

$$r^3 = \frac{2916\pi}{4\pi} = 729$$

Divide by 4π to isolate r.

$$r = \sqrt[3]{729} = 9$$

To undo cubing, take the cube root.

Problems

Use the given information to find the exact and approximate volume of the sphere.

1.
$$radius = 10 cm$$

2.
$$radius = 4 ft$$

3.
$$diameter = 10 cm$$

4.
$$diameter = 3 miles$$

5. circumference of great circle =
$$12\pi$$
 un.

6. circumference of great circle =
$$3\pi$$
 un.

Use the given information to answer each question related to spheres.

9. If the volume of the sphere is
$$36\pi$$
 un.³, find the radius.

10. If the volume of the sphere is
$$\frac{256\pi}{3}$$
 un.³, find the radius.

Answers

1.
$$\frac{4000\pi}{3} \approx 4186.67 \text{ cm}^3$$

3.
$$\frac{500\pi}{3} \approx 523.33 \text{ cm}^3$$

5.
$$288\pi \approx 904.32 \text{ un.}^3$$

7.
$$\frac{1372\pi}{3} \approx 1436.75 \text{ cm}^3$$

9.
$$r = 3$$
 units

2.
$$\frac{256\pi}{3} \approx 267.94 \text{ ft}^3$$

4.
$$\frac{9\pi}{2} \approx 14.13 \text{ mi}^3$$

6.
$$\frac{9\pi}{2} \approx 14.13 \text{ mi}^3$$

8.
$$\frac{500\pi}{3} \approx 523.60 \text{ in.}^3$$

10.
$$r = 4$$
 units